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# **mlpy Documentation**

***Release 3.5.0***

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**Homepage** <http://mlpy.sourceforge.net>

Machine Learning PYthon (mlpy) is a high-performance Python library for predictive modeling.

This reference manual details functions, modules, and objects included in mlpy.





## INSTALL

### 1.1 Download

Download latest version for your OS from <http://sourceforge.net/projects/mlpy/files/>

### 1.2 Installing on \*nix from source

On GNU/Linux, OSX and FreeBSD you need the following requirements:

- GCC
- Python >= 2.6 or 3.X
- NumPy >= 1.3.0 (with header files)
- SciPy >= 0.7.0
- GSL >= 1.11 (with header files)

From a terminal run:

```
$ python setup.py install
```

If you don't have root access, installing mlpy in a directory by specifying the `--prefix` argument. Then you need to set `PYTHONPATH`:

```
$ python setup.py install --prefix=/path/to/modules  
$ export PYTHONPATH=$PYTHONPATH:/path/to/modules/lib/python{version}/site-packages
```

If the GSL header files or shared library are in non-standard locations on your system, use the `--include-dirs` and `--rpath` options to `build_ext`:

```
$ python setup.py build_ext --include-dirs=/path/to/header --rpath=/path/to/lib  
$ python setup.py install
```

### 1.3 Installing on Windows Xp/Vista/7 from binary installer

Requirements:

- Python 2.6, 2.7, 3.1, 3.2 Windows installer (x86)
- NumPy >= 1.3.0 win32 installer

- SciPy  $\geq$  0.8.0 win32 installer

The GSL library is pre-compiled (by Visual Studio Express 2008) and included in mlpy.

Download and run the mlpy Windows installer (.exe).

## INTRODUCTION

### 2.1 Conventions

- $x$  is a matrix  $n \times p$  which represents a set of  $n$  samples in  $\mathbb{R}^p$ .
- $y$  is a vector  $n$  which represents the target values (integers in classification problems, floats in regression problems).



## TUTORIAL

If you are new in Python and NumPy see: <http://docs.python.org/tutorial/> [http://www.scipy.org/Tentative\\_NumPy\\_Tutorial](http://www.scipy.org/Tentative_NumPy_Tutorial) and <http://matplotlib.sourceforge.net/>.

A learning problem usually considers a set of  $p$ -dimensional samples (observations) of data and tries to predict properties of unknown data.

### 3.1 Tutorial 1 - Iris Dataset

The well known Iris dataset represents 3 kinds of Iris flowers with 150 observations and 4 attributes: sepal length, sepal width, petal length and petal width.

A dimensionality reduction and learning tasks can be performed by the `mlpy` library with just a few number of commands.

Download Iris dataset

Load the modules:

```
>>> import numpy as np
>>> import mlpy
>>> import matplotlib.pyplot as plt # required for plotting
```

Load the Iris dataset:

```
>>> iris = np.loadtxt('iris.csv', delimiter=',')
>>> x, y = iris[:, :4], iris[:, 4].astype(np.int) # x: (observations x attributes)
↳matrix, y: classes (1: setosa, 2: versicolor, 3: virginica)
>>> x.shape
(150, 4)
>>> y.shape
(150, )
```

Dimensionality reduction by Principal Component Analysis (PCA)

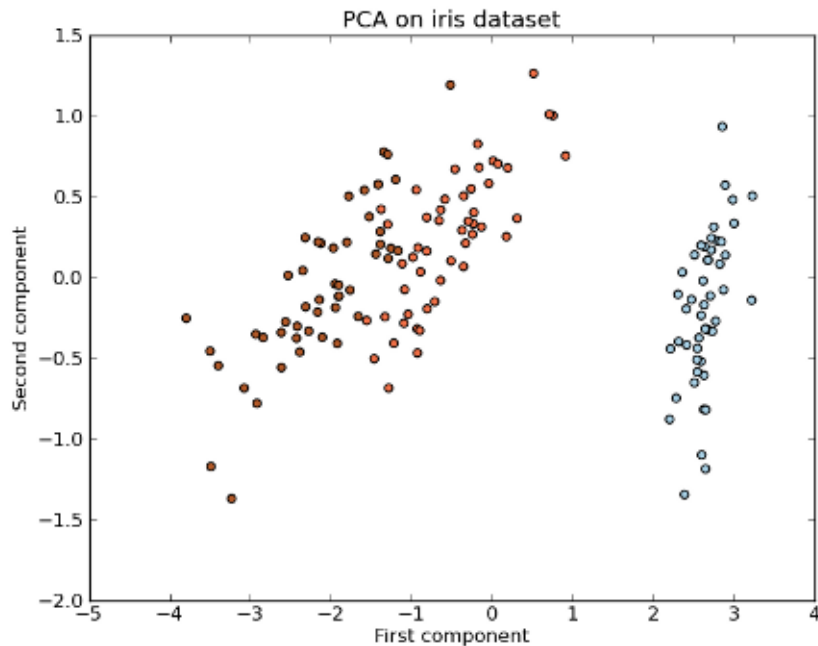
```
>>> pca = mlpy.PCA() # new PCA instance
>>> pca.learn(x) # learn from data
>>> z = pca.transform(x, k=2) # embed x into the k=2 dimensional subspace
>>> z.shape
(150, 2)
```

Plot the principal components:

```

>>> plt.set_cmap(plt.cm.Paired)
>>> fig1 = plt.figure(1)
>>> title = plt.title("PCA on iris dataset")
>>> plot = plt.scatter(z[:, 0], z[:, 1], c=y)
>>> labx = plt.xlabel("First component")
>>> laby = plt.ylabel("Second component")
>>> plt.show()

```



Learning by Kernel Support Vector Machines (SVMs) on principal components:

```

>>> linear_svm = mlpy.LibSvm(kernel_type='linear') # new linear SVM instance
>>> linear_svm.learn(z, y) # learn from principal components

```

For plotting purposes, we build the grid where we will compute the predictions (zgrid):

```

>>> xmin, xmax = z[:,0].min()-0.1, z[:,0].max()+0.1
>>> ymin, ymax = z[:,1].min()-0.1, z[:,1].max()+0.1
>>> xx, yy = np.meshgrid(np.arange(xmin, xmax, 0.01), np.arange(ymin, ymax, 0.01))
>>> zgrid = np.c_[xx.ravel(), yy.ravel()]

```

Now we perform the predictions on the grid. The `pred()` method returns the prediction for each point in zgrid:

```

>>> yp = linear_svm.pred(zgrid)

```

Plot the predictions:

```

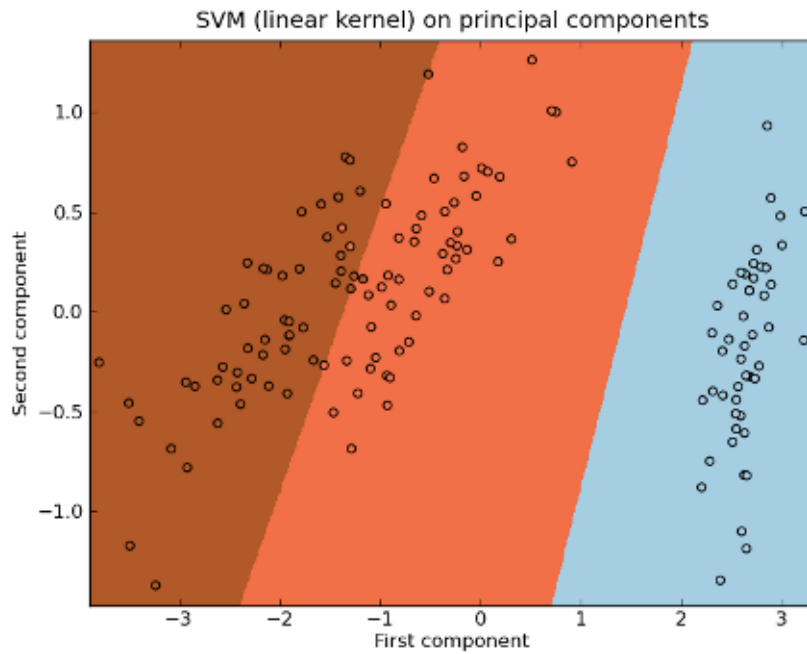
>>> plt.set_cmap(plt.cm.Paired)
>>> fig2 = plt.figure(2)
>>> title = plt.title("SVM (linear kernel) on principal components")
>>> plot1 = plt.pcolormesh(xx, yy, yp.reshape(xx.shape))
>>> plot2 = plt.scatter(z[:, 0], z[:, 1], c=y)
>>> labx = plt.xlabel("First component")

```

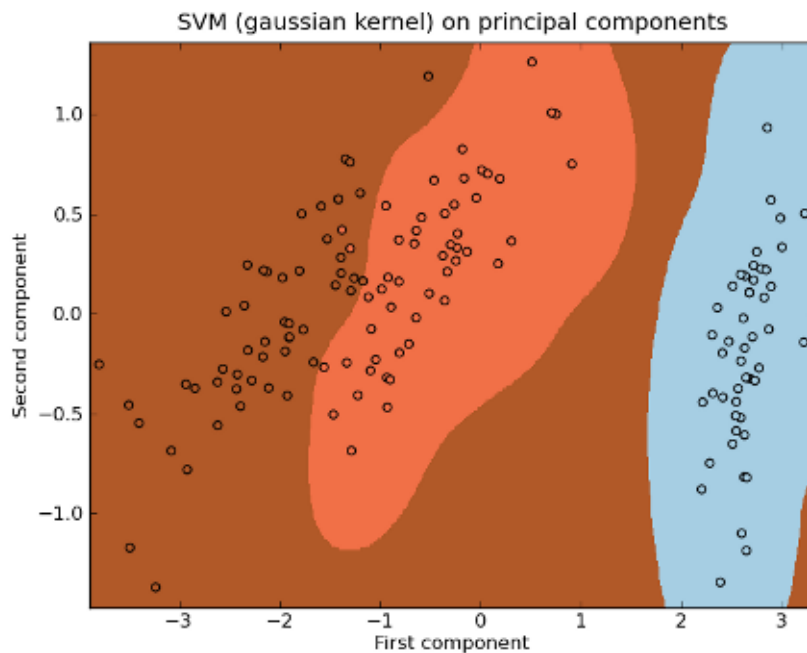
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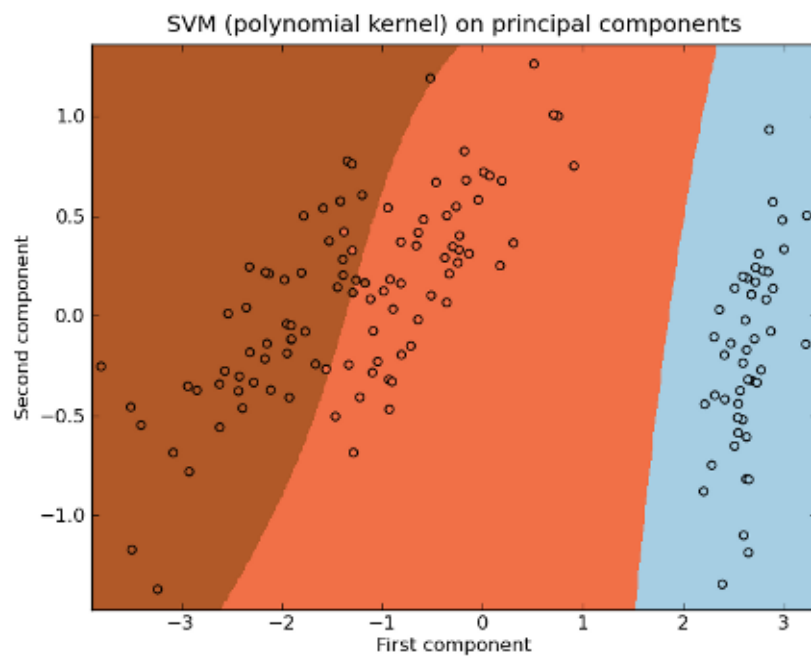
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```
>>> laby = plt.ylabel("Second component")
>>> limx = plt.xlim(xmin, xmax)
>>> limy = plt.ylim(ymin, ymax)
>>> plt.show()
```



We can try to use different kernels to obtain:





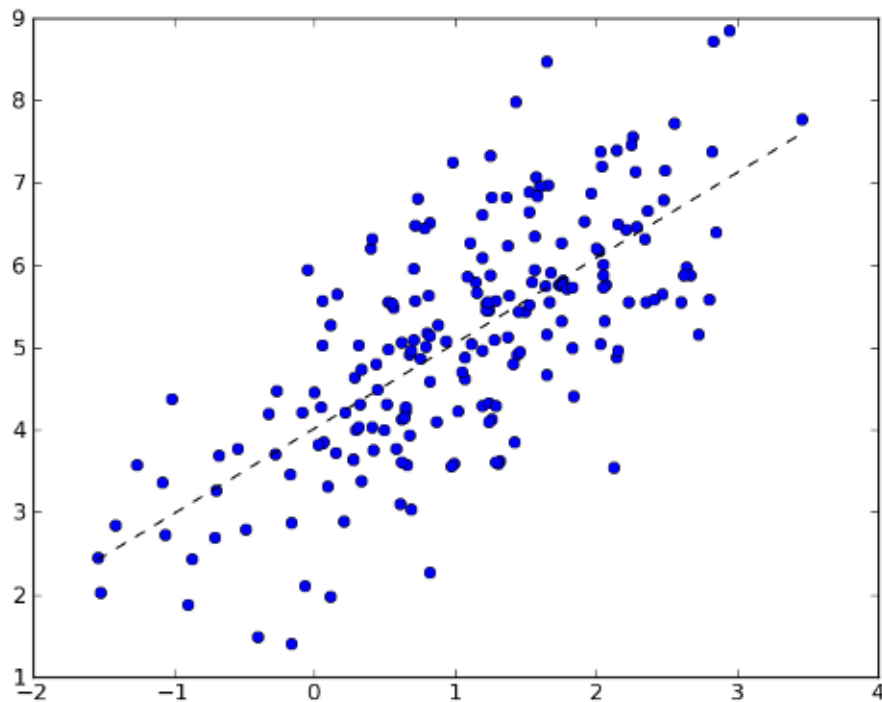


## LINEAR METHODS FOR REGRESSION

### 4.1 Ordinary Least Squares

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlp
>>> np.random.seed(0)
>>> mean, cov, n = [1, 5], [[1,1],[1,2]], 200
>>> d = np.random.multivariate_normal(mean, cov, n)
>>> x, y = d[:, 0].reshape(-1, 1), d[:, 1]
>>> x.shape
(200, 1)
>>> ols = mlp.OLS()
>>> ols.learn(x, y)
>>> xx = np.arange(np.min(x), np.max(x), 0.01).reshape(-1, 1)
>>> yy = ols.pred(xx)
>>> fig = plt.figure(1) # plot
>>> plot = plt.plot(x, y, 'o', xx, yy, '--k')
>>> plt.show()
```

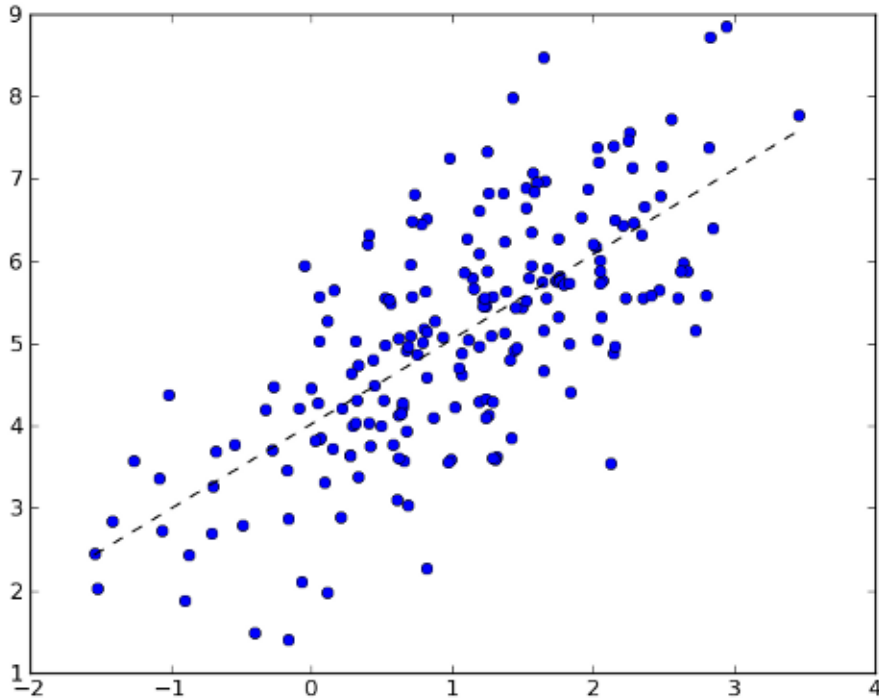


## 4.2 Ridge Regression

See [Hoerl70]. Ridge regression is also known as regularized least squares. It avoids overfitting by controlling the size of the model vector  $\beta$ , measured by its  $\ell^2$ -norm.

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean, cov, n = [1, 5], [[1,1],[1,2]], 200
>>> d = np.random.multivariate_normal(mean, cov, n)
>>> x, y = d[:, 0].reshape(-1, 1), d[:, 1]
>>> x.shape
(200, 1)
>>> ridge = mlpy.Ridge()
>>> ridge.learn(x, y)
>>> xx = np.arange(np.min(x), np.max(x), 0.01).reshape(-1, 1)
>>> yy = ridge.pred(xx)
>>> fig = plt.figure(1) # plot
>>> plot = plt.plot(x, y, 'o', xx, yy, '--k')
>>> plt.show()
```



### 4.3 Partial Least Squares

### 4.4 Last Angle Regression (LARS)

This example replicates the Figure 3 in [Efron04]. The diabetes data can be downloaded from <http://www.stanford.edu/~hastie/Papers/LARS/diabetes.data>

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> diabetes = np.loadtxt("diabetes.data", skiprows=1)
>>> x = diabetes[:, :-1]
>>> y = diabetes[:, -1]
>>> x -= np.mean(x, axis=0) # center x
>>> x /= np.sqrt(np.sum((x)**2, axis=0)) # normalize x
>>> y -= np.mean(y) # center y
>>> lars = mlpy.LARS()
>>> lars.learn(x, y)
>>> lars.steps() # number of steps performed
10
>>> lars.beta()
array([-10.0098663 , -239.81564367,  519.84592005,  324.3846455 ,
       -792.17563855,  476.73902101,  101.04326794,  177.06323767,
        751.27369956,   67.62669218])
>>> lars.beta0()
```

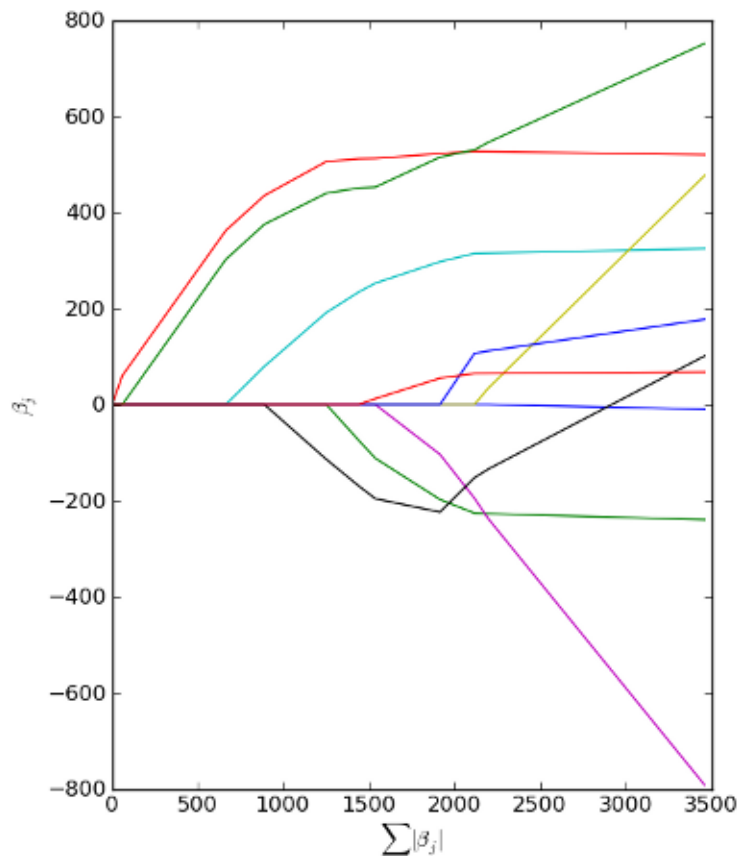
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```

4.7406304540474682e-14
>>> est = lars.est() # returns all LARS estimates
>>> beta_sum = np.sum(np.abs(est), axis=1)
>>> fig = plt.figure(1)
>>> plot1 = plt.plot(beta_sum, est)
>>> x1 = plt.xlabel(r'$\sum{|\beta_j|}$')
>>> y1 = plt.ylabel(r'$\beta_j$')
>>> plt.show()

```



## 4.5 Elastic Net

Documentation and implementation is taken from <http://web.mit.edu/iroasco/www/contents/code/ENcode.html>

Computes the coefficient vector which solves the elastic-net regularization problem

$$\min\{\|X\beta - Y\|^2 + \lambda(\|\beta\|_2^2 + \epsilon\|\beta\|_1)\}$$

Elastic Net Regularization is an algorithm for learning and variable selection. It is based on a regularized least square procedure with a penalty which is the sum of an L1 penalty (like Lasso) and an L2 penalty (like ridge regression). The first term enforces the sparsity of the solution, whereas the second term ensures democracy among groups of correlated variables. The second term has also a smoothing effect that stabilizes the obtained solution.

## LINEAR METHODS FOR CLASSIFICATION

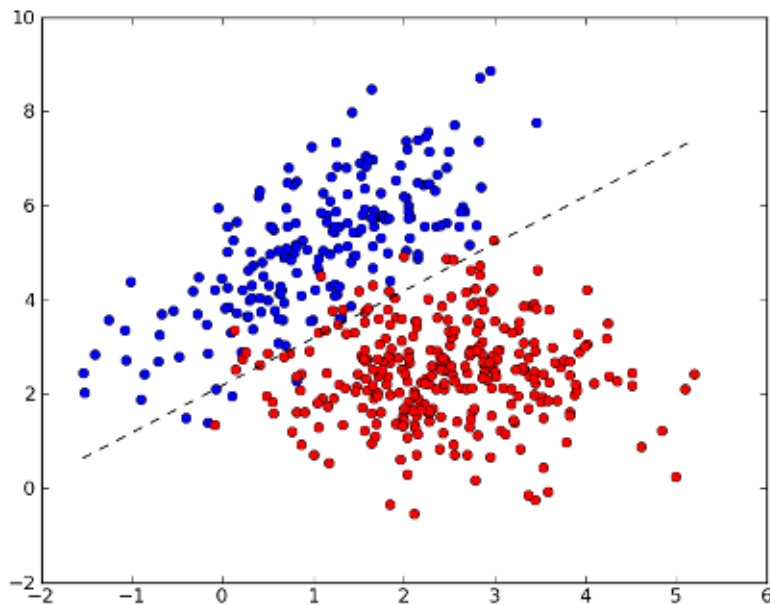
### 5.1 Linear Discriminant Analysis Classifier (LDAC)

See [Hastie09], page 106.

#### 5.1.1 Examples

Binary classification:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlp
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 5], [[1,1],[1,2]], 200 # 200 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,0],[0,1]], 300 # 300 samples of class -1
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = -np.ones(n2, dtype=np.int)
>>> x = np.concatenate((x1, x2), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2))
>>> ldac = mlp.LDAC()
>>> ldac.learn(x, y)
>>> w = ldac.w()
>>> w
array([ 2.5948979 -2.58553746])
>>> b = ldac.bias()
>>> b
5.63727441841
>>> xx = np.arange(np.min(x[:,0]), np.max(x[:,0]), 0.01)
>>> yy = - (w[0] * xx + b) / w[1] # separator line
>>> fig = plt.figure(1) # plot
>>> plot1 = plt.plot(x1[:, 0], x1[:, 1], 'ob', x2[:, 0], x2[:, 1], 'or')
>>> plot2 = plt.plot(xx, yy, '--k')
>>> plt.show()
```



```
>>> test = [[0, 2], [4, 2]] # test points
>>> ldac.pred(test)
array([-1, -1])
>>> ldac.labels()
array([-1, 1])
```

Multiclass classification:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 25], [[1,1],[1,2]], 200 # 200 samples of class 0
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.zeros(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 22.5], [[1,0],[0,1]], 300 # 300 samples of class 1
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = np.ones(n2, dtype=np.int)
>>> mean3, cov3, n3 = [5, 28], [[0.5,0],[0,0.5]], 200 # 200 samples of class 2
>>> x3 = np.random.multivariate_normal(mean3, cov3, n3)
>>> y3 = 2 * np.ones(n3, dtype=np.int)
>>> x = np.concatenate((x1, x2, x3), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2, y3))
>>> ldac = mlpy.LDAC()
>>> ldac.learn(x, y)
>>> w = ldac.w()
>>> w # w[i]: coefficients label ldac.labels()[i]
array([[ -0.30949939  4.53041257]
       [ 2.52002288  1.50501818]
       [ 4.2499381   5.90569921]])
>>> b = ldac.bias()
>>> b # b[i]: bias for label ldac.labels()[i]
array([-12.65129158 -5.7628039 -35.63605709])
```

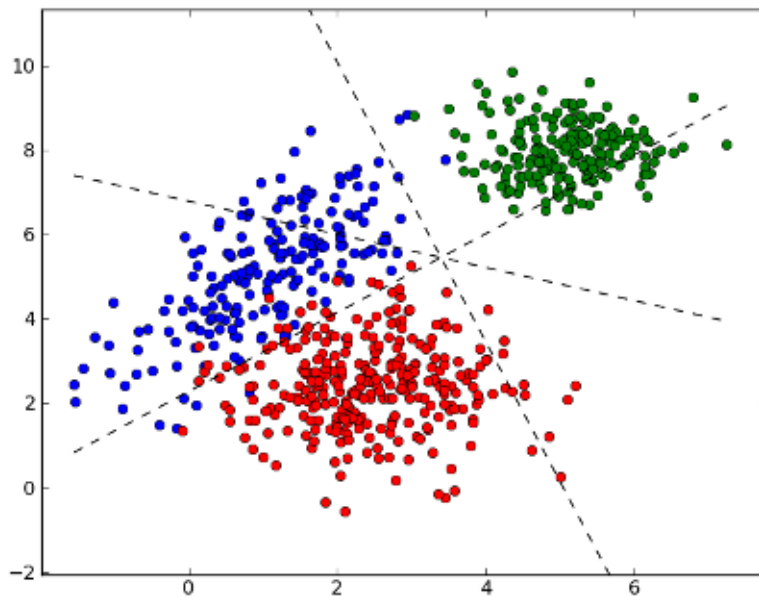
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```

>>> xx = np.arange(np.min(x[:,0]), np.max(x[:,0]), 0.01)
>>> yy1 = (xx * (w[1][0]-w[0][0]) + b[1] - b[0]) / (w[0][1]-w[1][1])
>>> yy2 = (xx * (w[2][0]-w[0][0]) + b[2] - b[0]) / (w[0][1]-w[2][1])
>>> yy3 = (xx * (w[2][0]-w[1][0]) + b[2] - b[1]) / (w[1][1]-w[2][1])
>>> fig = plt.figure(1) # plot
>>> plot1 = plt.plot(x1[:, 0], x1[:, 1], 'ob', x2[:, 0], x2[:, 1], 'or', x3[:, 0],
↳ x3[:, 1], 'og')
>>> plot2 = plt.plot(xx, yy1, '--k')
>>> plot3 = plt.plot(xx, yy2, '--k')
>>> plot4 = plt.plot(xx, yy3, '--k')
>>> plt.show()

```



```

>>> test = [[6,7], [4, 2]] # test points
>>> ldac.pred(test)
array([2, 1])
>>> ldac.labels()
array([0, 1, 2])

```

## 5.2 Basic Perceptron

### 5.2.1 Examples

```

>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 5], [[1,1],[1,2]], 200 # 200 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)

```

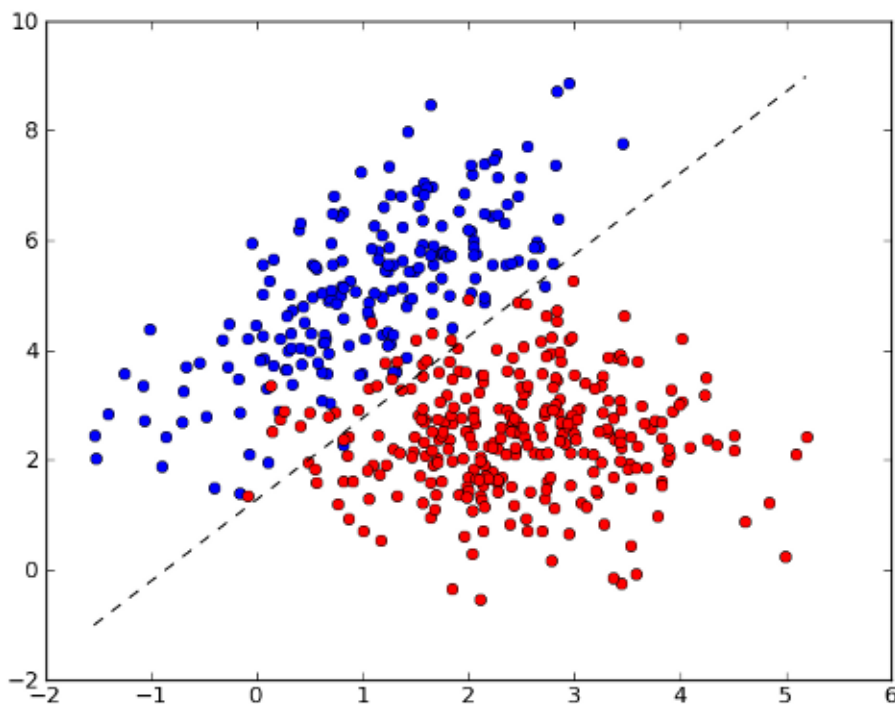
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```

>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,0],[0,1]], 300 # 300 samples of class -1
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = -np.ones(n2, dtype=np.int)
>>> x = np.concatenate((x1, x2), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2))
>>> p = mlpy.Perceptron(alpha=0.1, thr=0.05, maxiters=100) # basic perceptron
>>> p.learn(x, y)
>>> w = p.w()
>>> w
array([-69.00185254,  46.49202132])
>>> b = p.bias()
>>> b
-59.600000000000001
>>> p.err()
0.050000000000000003
>>> p.iters()
46
>>> xx = np.arange(np.min(x[:,0]), np.max(x[:,0]), 0.01)
>>> yy = - (w[0] * xx + b) / w[1] # separator line
>>> fig = plt.figure(1) # plot
>>> plot1 = plt.plot(x1[:, 0], x1[:, 1], 'ob', x2[:, 0], x2[:, 1], 'or')
>>> plot2 = plt.plot(xx, yy, '--k')
>>> plt.show()

```



```

>>> test = [[0, 2], [4, 2]] # test points
>>> p.pred(test)

```

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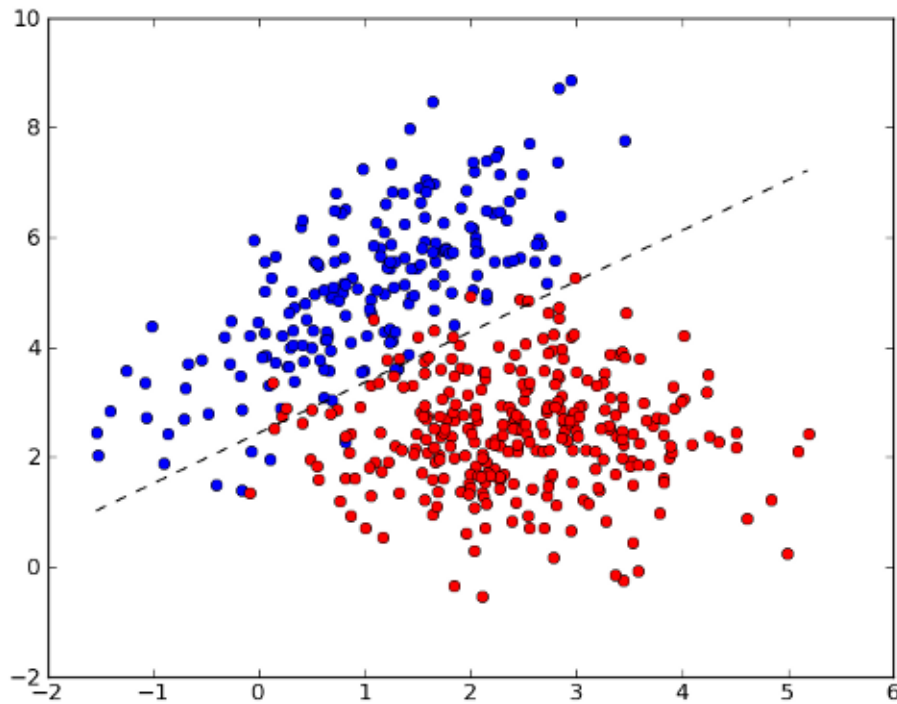
```
array([ 1, -1])
>>> p.labels()
array([-1,  1])
```

## 5.3 Elastic Net Classifier

See [Hastie09], Chapter 18, page 661.

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 5], [[1,1],[1,2]], 200 # 200 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,0],[0,1]], 300 # 300 samples of class -1
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = -np.ones(n2, dtype=np.int)
>>> x = np.concatenate((x1, x2), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2))
>>> en = mlpy.ElasticNetC(lmb=0.01, eps=0.001)
>>> en.learn(x, y)
>>> w = en.w()
>>> w
array([-0.27733363,  0.30115026])
>>> b = en.bias()
>>> b
-0.73445916200332606
>>> en.iters()
1000
>>> xx = np.arange(np.min(x[:,0]), np.max(x[:,0]), 0.01)
>>> yy = - (w[0] * xx + b) / w[1] # separator line
>>> fig = plt.figure(1) # plot
>>> plot1 = plt.plot(x1[:, 0], x1[:, 1], 'ob', x2[:, 0], x2[:, 1], 'or')
>>> plot2 = plt.plot(xx, yy, '--k')
>>> plt.show()
```



```
>>> test = [[1, 4], [2, 2]] # test points
>>> en.pred(test)
array([ 1., -1.])
```

## 5.4 Logistic Regression

See *Large Linear Classification from [LIBLINEAR]*

## 5.5 Support Vector Classification

See *Large Linear Classification from [LIBLINEAR]*

## 5.6 Diagonal Linear Discriminant Analysis (DLDA)

See [Hastie09], page 651.

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
```

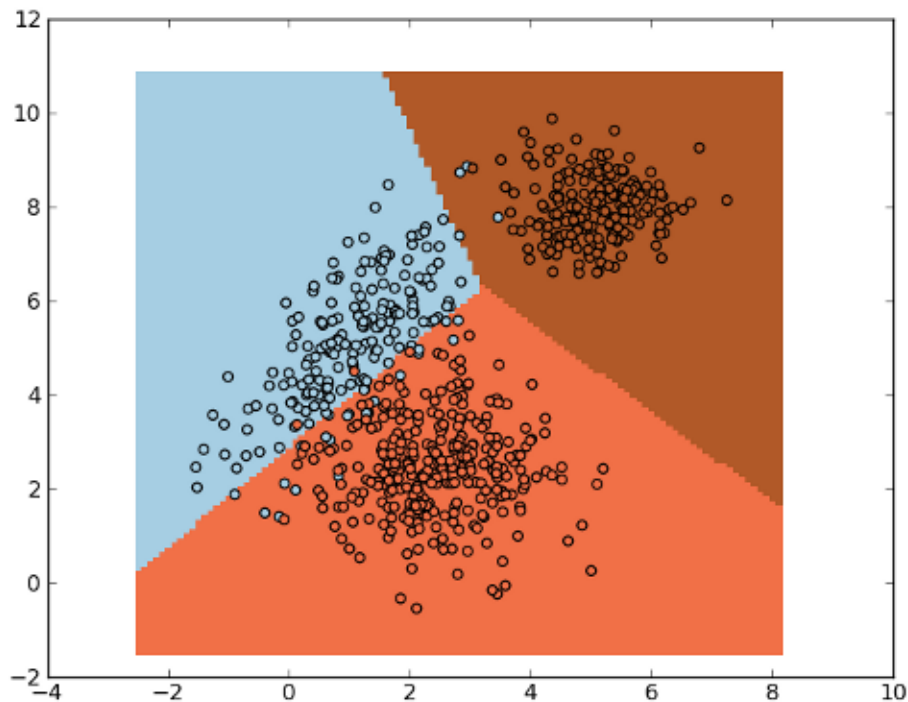
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```

>>> mean1, cov1, n1 = [1, 5], [[1,1],[1,2]], 200 # 200 samples of class 0
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.zeros(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,0],[0,1]], 300 # 300 samples of class 1
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = np.ones(n2, dtype=np.int)
>>> mean3, cov3, n3 = [5, 8], [[0.5,0],[0,0.5]], 200 # 200 samples of class 2
>>> x3 = np.random.multivariate_normal(mean3, cov3, n3)
>>> y3 = 2 * np.ones(n3, dtype=np.int)
>>> x = np.concatenate((x1, x2, x3), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2, y3))
>>> da = mlpy.DLDA(delta=0.1)
>>> da.learn(x, y)
>>> xmin, xmax = x[:,0].min()-1, x[:,0].max()+1
>>> ymin, ymax = x[:,1].min()-1, x[:,1].max()+1
>>> xx, yy = np.meshgrid(np.arange(xmin, xmax, 0.1), np.arange(ymin, ymax, 0.1))
>>> xnew = np.c_[xx.ravel(), yy.ravel()]
>>> ynew = da.pred(xnew).reshape(xx.shape)
>>> fig = plt.figure(1)
>>> cmap = plt.set_cmap(plt.cm.Paired)
>>> plot1 = plt.pcolormesh(xx, yy, ynew)
>>> plot2 = plt.scatter(x[:,0], x[:,1], c=y)
>>> plt.show()

```



## 5.7 Golub Classifier



## KERNELS

## 6.1 Kernel Functions

A kernel is a function  $\kappa$  that for all  $\mathbf{t}, \mathbf{x} \in X$  satisfies  $\kappa(\mathbf{t}, \mathbf{x}) = \langle \Phi(\mathbf{t}), \Phi(\mathbf{x}) \rangle$ , where  $\Phi$  is a mapping from  $X$  to an (inner product) feature space  $F$ ,  $\Phi : \mathbf{t} \mapsto \Phi(\mathbf{t}) \in F$ .

The following functions take two array-like objects  $\mathbf{t}$  (M, P) and  $\mathbf{x}$  (N, P) and compute the (M, N) matrix  $\mathbf{K}^t$  with entries

$$\mathbf{K}^t_{ij} = \kappa(\mathbf{t}_i, \mathbf{x}_j).$$

## 6.2 Kernel Classes

## 6.3 Functions

```
mlpy.kernel_linear(t, x)
    Linear kernel,  $\mathbf{t}_i' \mathbf{x}_j$ .

mlpy.kernel_polynomial(t, x, gamma=1.0, b=1.0, d=2.0)
    Polynomial kernel,  $(\text{gamma } \mathbf{t}_i' \mathbf{x}_j + b)^d$ .

mlpy.kernel_gaussian(t, x, sigma=1.0)
    Gaussian kernel,  $\exp(-\|\mathbf{t}_i - \mathbf{x}_j\|^2 / 2 * \text{sigma}^2)$ .

mlpy.kernel_exponential(t, x, sigma=1.0)
    Exponential kernel,  $\exp(-\|\mathbf{t}_i - \mathbf{x}_j\| / 2 * \text{sigma}^2)$ .

mlpy.kernel_sigmoid(t, x, gamma=1.0, b=1.0)
    Sigmoid kernel,  $\tanh(\text{gamma } \mathbf{t}_i' \mathbf{x}_j + b)$ .
```

Example:

```
>>> import mlpy
>>> x = [[5, 1, 3, 1], [7, 1, 11, 4], [0, 4, 2, 9]] # three training points
>>> K = mlpy.kernel_gaussian(x, x, sigma=10) # compute the kernel matrix  $K_{ij} = k(\mathbf{x}_i,$ 
    ↪  $\mathbf{x}_j)$ 
>>> K
array([[ 1.,          0.68045064,  0.60957091],
       [ 0.68045064,  1.,          0.44043165],
       [ 0.60957091,  0.44043165,  1.]])
```

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```

>>> t = [[8, 1, 5, 1], [7, 1, 11, 4]] # two test points
>>> Kt = mlpy.kernel_gaussian(t, x, sigma=10) # compute the test kernel matrix Kt_ij
↪ = <Phi(t_i), Phi(x_j)> = k(t_i, x_j)
>>> Kt
array([[ 0.93706746,  0.7945336 ,  0.48190899],
       [ 0.68045064,  1.         ,  0.44043165]])

```

## 6.4 Centering in Feature Space

The centered kernel matrix  $\tilde{\mathbf{K}}^t$  is computed by:

$$\tilde{\mathbf{K}}_{ij}^t = \left\langle \Phi(\mathbf{t}_i) - \frac{1}{N} \sum_{m=1}^N \Phi(\mathbf{x}_m), \Phi(\mathbf{x}_j) - \frac{1}{N} \sum_{n=1}^N \Phi(\mathbf{x}_n) \right\rangle.$$

We can express  $\tilde{\mathbf{K}}^t$  in terms of  $\mathbf{K}^t$  and  $\mathbf{K}$ :

$$\tilde{\mathbf{K}}_{ij}^t = \mathbf{K}^t - \mathbf{1}_N^T \mathbf{K} - \mathbf{K}^t \mathbf{1}_N + \mathbf{1}_N^T \mathbf{K} \mathbf{1}_N$$

where  $\mathbf{1}_N$  is the  $N \times M$  matrix with all entries equal to  $1/N$  and  $\mathbf{K}$  is  $\mathbf{K}_{ij} = \kappa(\mathbf{x}_i, \mathbf{x}_j)$ .

`mlpy.kernel_center(Kt, K)`

Centers the testing kernel matrix Kt respect the training kernel matrix K. If  $\mathbf{K}t = \mathbf{K}$  (`kernel_center(K, K)`), where  $\mathbf{K} = \mathbf{k}(\mathbf{x}_i, \mathbf{x}_j)$ , the function centers the kernel matrix K.

### Parameters

**Kt** [2d array\_like object (M, N)] test kernel matrix  $\mathbf{K}t_{ij} = \mathbf{k}(\mathbf{t}_i, \mathbf{x}_j)$ . If  $\mathbf{K}t = \mathbf{K}$  the function centers the kernel matrix K

**K** [2d array\_like object (N, N)] training kernel matrix  $\mathbf{K}_{ij} = \mathbf{k}(\mathbf{x}_i, \mathbf{x}_j)$

### Returns

**Ktcentered** [2d numpy array (M, N)] centered version of Kt

Example:

```

>>> Kcentered = mlpy.kernel_center(K, K) # center K
>>> Kcentered
array([[ 0.19119746, -0.07197215, -0.11922531],
       [-0.07197215,  0.30395696, -0.23198481],
       [-0.11922531, -0.23198481,  0.35121011]])
>>> Ktcentered = mlpy.kernel_center(Kt, K) # center the test kernel matrix Kt respect
↪ to K
>>> Ktcentered
array([[ 0.15376875,  0.06761464, -0.22138339],
       [-0.07197215,  0.30395696, -0.23198481]])

```

## 6.5 Make a Custom Kernel

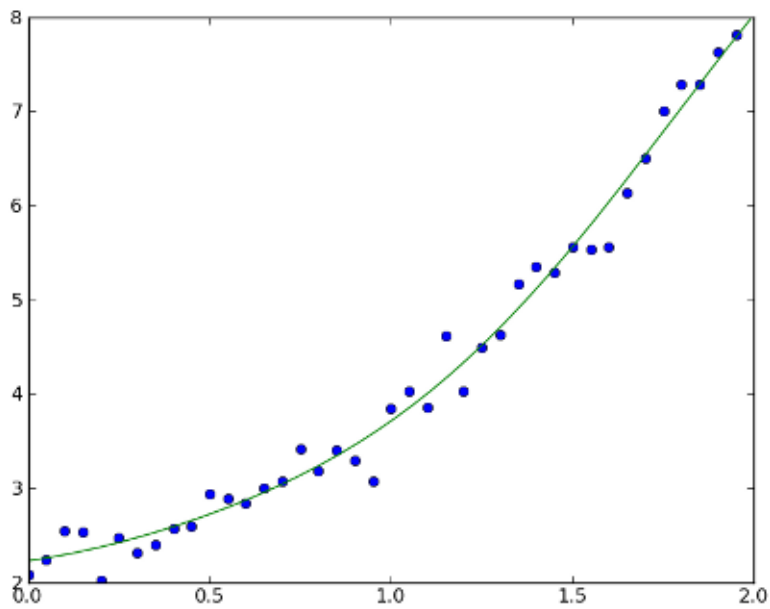
TODO

## NON LINEAR METHODS FOR REGRESSION

### 7.1 Kernel Ridge Regression

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> x = np.arange(0, 2, 0.05).reshape(-1, 1) # training points
>>> y = np.ravel(np.exp(x)) + np.random.normal(1, 0.2, x.shape[0]) # target values
>>> xt = np.arange(0, 2, 0.01).reshape(-1, 1) # testing points
>>> K = mlpy.kernel_gaussian(x, x, sigma=1) # training kernel matrix
>>> Kt = mlpy.kernel_gaussian(xt, x, sigma=1) # testing kernel matrix
>>> krr = KernelRidge(lmb=0.01)
>>> krr.learn(K, y)
>>> yt = krr.pred(Kt)
>>> fig = plt.figure(1)
>>> plot1 = plt.plot(x[:, 0], y, 'o')
>>> plot2 = plt.plot(xt[:, 0], yt)
>>> plt.show()
```



## 7.2 Support Vector Regression

See *Support Vector Machines (SVMs)*

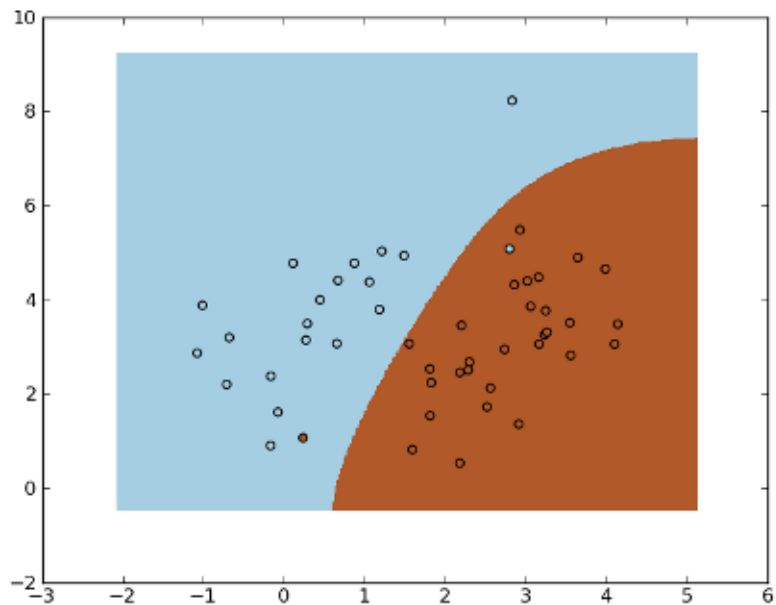


## NON LINEAR METHODS FOR CLASSIFICATION

### 8.1 Parzen-based classifier

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlp
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 4.5], [[1,1],[1,2]], 20 # 20 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,1],[1,2]], 30 # 30 samples of class 2
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = 2 * np.ones(n2, dtype=np.int)
>>> x = np.concatenate((x1, x2), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2))
>>> K = mlp.kernel_gaussian(x, x, sigma=2) # kernel matrix
>>> parzen = mlp.Parzen()
>>> parzen.learn(K, y)
>>> xmin, xmax = x[:,0].min()-1, x[:,0].max()+1
>>> ymin, ymax = x[:,1].min()-1, x[:,1].max()+1
>>> xx, yy = np.meshgrid(np.arange(xmin, xmax, 0.02), np.arange(ymin, ymax, 0.02))
>>> xt = np.c_[xx.ravel(), yy.ravel()] # test points
>>> Kt = mlp.kernel_gaussian(xt, x, sigma=2) # test kernel matrix
>>> yt = parzen.pred(Kt).reshape(xx.shape)
>>> fig = plt.figure(1)
>>> cmap = plt.set_cmap(plt.cm.Paired)
>>> plot1 = plt.pcolormesh(xx, yy, yt)
>>> plot2 = plt.scatter(x[:,0], x[:,1], c=y)
>>> plt.show()
```



## 8.2 Support Vector Classification

See *Support Vector Machines (SVMs)*

## 8.3 Kernel Fisher Discriminant Classifier

## 8.4 k-Nearest-Neighbor

**class** mlpy.KNN(*k*)  
k-Nearest Neighbor (euclidean distance)

### Parameters

**k** [int] number of nearest neighbors

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 5], [[1,1],[1,2]], 200 # 200 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,0],[0,1]], 300 # 300 samples of class 2
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = 2 * np.ones(n2, dtype=np.int)
>>> mean3, cov3, n3 = [5, 8], [[0.5,0],[0,0.5]], 200 # 200 samples of class 3
```

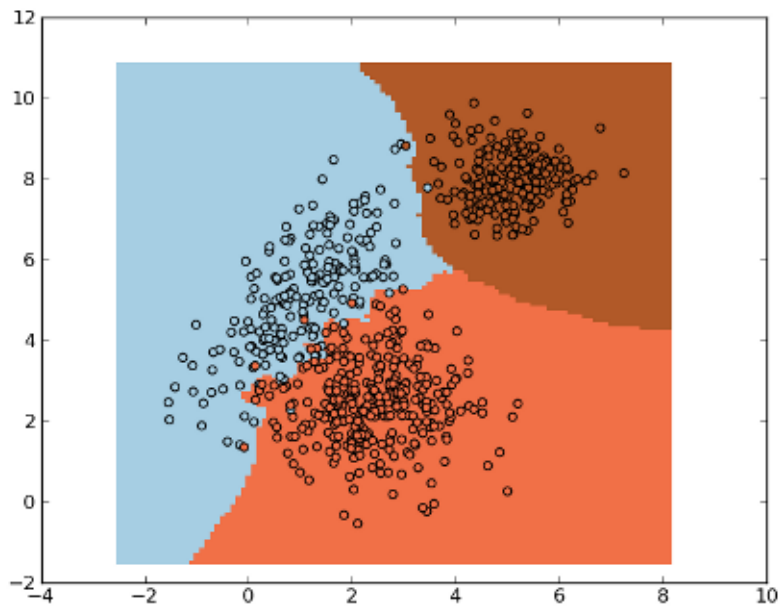
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```

>>> x3 = np.random.multivariate_normal(mean3, cov3, n3)
>>> y3 = 3 * np.ones(n3, dtype=np.int)
>>> x = np.concatenate((x1, x2, x3), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2, y3))
>>> knn = mlpy.KNN(k=3)
>>> knn.learn(x, y)
>>> xmin, xmax = x[:,0].min()-1, x[:,0].max()+1
>>> ymin, ymax = x[:,1].min()-1, x[:,1].max()+1
>>> xx, yy = np.meshgrid(np.arange(xmin, xmax, 0.1), np.arange(ymin, ymax, 0.1))
>>> xnew = np.c_[xx.ravel(), yy.ravel()]
>>> ynew = knn.pred(xnew).reshape(xx.shape)
>>> ynew[ynew == 0] = 1 # set the samples with no unique classification to 1
>>> fig = plt.figure(1)
>>> cmap = plt.set_cmap(plt.cm.Paired)
>>> plot1 = plt.pcolormesh(xx, yy, ynew)
>>> plot2 = plt.scatter(x[:,0], x[:,1], c=y)
>>> plt.show()

```



## 8.5 Classification Tree

**class** mlpy.ClassTree (stumps=0, minsize=1)  
Classification Tree (gini index)

### Parameters

**stumps** [bool] True: compute single split or False: standard tree

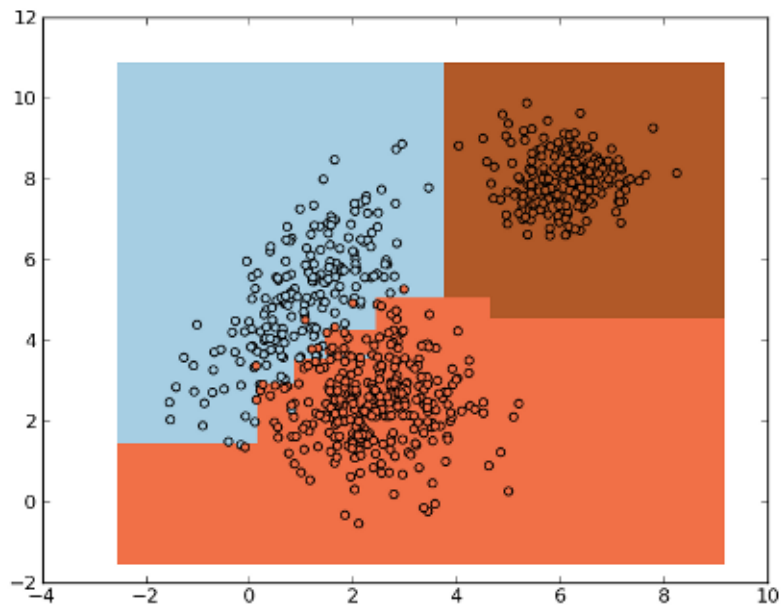
**minsize** [int (>=0)] minimum number of cases required to split a leaf

Example:

```

>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 5], [[1,1],[1,2]], 200 # 200 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,0],[0,1]], 300 # 300 samples of class 2
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = 2 * np.ones(n2, dtype=np.int)
>>> mean3, cov3, n3 = [6, 8], [[0.5,0],[0,0.5]], 200 # 200 samples of class 3
>>> x3 = np.random.multivariate_normal(mean3, cov3, n3)
>>> y3 = 3 * np.ones(n3, dtype=np.int)
>>> x = np.concatenate((x1, x2, x3), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2, y3))
>>> tree = mlpy.ClassTree(minsize=10)
>>> tree.learn(x, y)
>>> xmin, xmax = x[:,0].min()-1, x[:,0].max()+1
>>> ymin, ymax = x[:,1].min()-1, x[:,1].max()+1
>>> xx, yy = np.meshgrid(np.arange(xmin, xmax, 0.1), np.arange(ymin, ymax, 0.1))
>>> xnew = np.c_[xx.ravel(), yy.ravel()]
>>> ynew = tree.pred(xnew).reshape(xx.shape)
>>> ynew[ynew == 0] = 1 # set the samples with no unique classification to 1
>>> fig = plt.figure(1)
>>> cmap = plt.set_cmap(plt.cm.Paired)
>>> plot1 = plt.pcolormesh(xx, yy, ynew)
>>> plot2 = plt.scatter(x[:,0], x[:,1], c=y)
>>> plt.show()

```

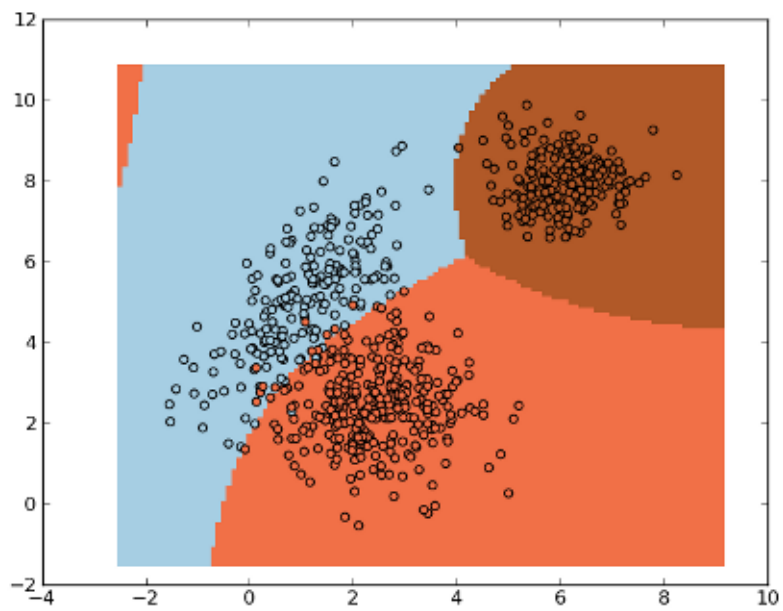


## 8.6 Maximum Likelihood Classifier

**class** mlpy.MaximumLikelihoodC  
Maximum Likelihood Classifier

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 5], [[1,1],[1,2]], 200 # 200 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,0],[0,1]], 300 # 300 samples of class 2
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = 2 * np.ones(n2, dtype=np.int)
>>> mean3, cov3, n3 = [6, 8], [[0.5,0],[0,0.5]], 200 # 200 samples of class 3
>>> x3 = np.random.multivariate_normal(mean3, cov3, n3)
>>> y3 = 3 * np.ones(n3, dtype=np.int)
>>> x = np.concatenate((x1, x2, x3), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2, y3))
>>> ml = mlpy.MaximumLikelihoodC()
>>> ml.learn(x, y)
>>> xmin, xmax = x[:,0].min()-1, x[:,0].max()+1
>>> ymin, ymax = x[:,1].min()-1, x[:,1].max()+1
>>> xx, yy = np.meshgrid(np.arange(xmin, xmax, 0.1), np.arange(ymin, ymax, 0.1))
>>> xnew = np.c_[xx.ravel(), yy.ravel()]
>>> ynew = ml.pred(xnew).reshape(xx.shape)
>>> ynew[ynew == 0] = 1 # set the samples with no unique classification to 1
>>> fig = plt.figure(1)
>>> cmap = plt.set_cmap(plt.cm.Paired)
>>> plot1 = plt.pcolormesh(xx, yy, ynew)
>>> plot2 = plt.scatter(x[:,0], x[:,1], c=y)
>>> plt.show()
```



## SUPPORT VECTOR MACHINES (SVMS)

### 9.1 Support Vector Machines from [LIBSVM]

```
class mlpy.LibSvm(svm_type='c_svc', kernel_type='linear', degree=3, gamma=0.001, coef0=0, C=1,
                  nu=0.5, eps=0.001, p=0.1, cache_size=100, shrinking=True, probability=False,
                  weight={})
```

LibSvm.

#### Parameters

**svm\_type** [string] SVM type, can be one of: 'c\_svc', 'nu\_svc', 'one\_class', 'epsilon\_svr', 'nu\_svr'

**kernel\_type** [string] kernel type, can be one of: 'linear' ( $u^T v$ ), 'poly' ( $((\gamma u^T v + \text{coef0})^{\text{degree}})$ ), 'rbf' ( $\exp(-\gamma \|u - v\|^2)$ ), 'sigmoid' ( $\tanh(\gamma u^T v + \text{coef0})$ )

**degree** [int (for 'poly' kernel\_type)] degree in kernel

**gamma** [float (for 'poly', 'rbf', 'sigmoid' kernel\_type)] gamma in kernel (e.g.  $1 / \text{number of features}$ )

**coef0** [float (for 'poly', 'sigmoid' kernel\_type)] coef0 in kernel

**C** [float (for 'c\_svc', 'epsilon\_svr', 'nu\_svr')] cost of constraints violation

**nu** [float (for 'nu\_svc', 'one\_class', 'nu\_svr')] nu parameter

**eps** [float] stopping criterion, usually 0.00001 in nu-SVC, 0.001 in others

**p** [float (for 'epsilon\_svr')] p is the epsilon in epsilon-insensitive loss function of epsilon-SVM regression

**cache\_size** [float [MB]] size of the kernel cache, specified in megabytes

**shrinking** [bool] use the shrinking heuristics

**probability** [bool] predict probability estimates

**weight** [dict] changes the penalty for some classes (if the weight for a class is not changed, it is set to 1). For example, to change penalty for classes 1 and 2 to 0.5 and 0.8 respectively set `weight={1:0.5, 2:0.8}`

Example on spiral dataset:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> f = np.loadtxt("spiral.data")
>>> x, y = f[:, :2], f[:, 2]
```

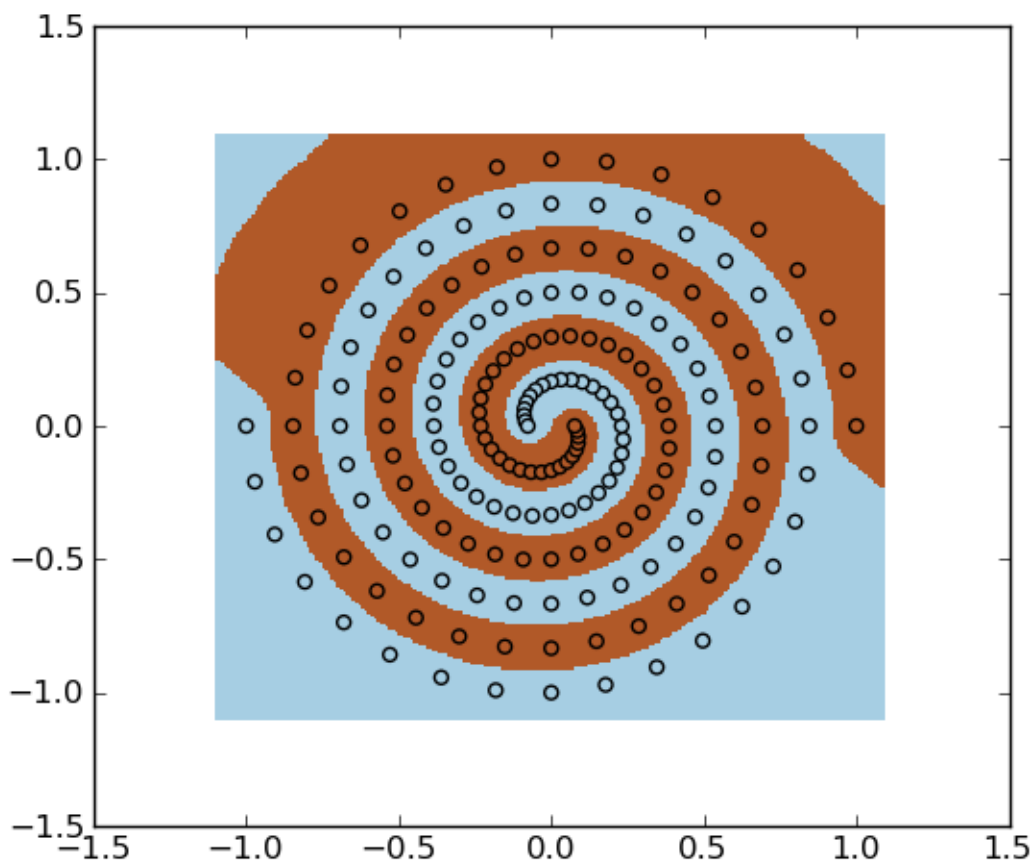
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```

>>> svm = mlpy.LibSvm(svm_type='c_svc', kernel_type='rbf', gamma=100)
>>> svm.learn(x, y)
>>> xmin, xmax = x[:,0].min()-0.1, x[:,0].max()+0.1
>>> ymin, ymax = x[:,1].min()-0.1, x[:,1].max()+0.1
>>> xx, yy = np.meshgrid(np.arange(xmin, xmax, 0.01), np.arange(ymin, ymax, 0.01))
>>> xnew = np.c_[xx.ravel(), yy.ravel()]
>>> ynew = svm.pred(xnew).reshape(xx.shape)
>>> fig = plt.figure(1)
>>> plt.set_cmap(plt.cm.Paired)
>>> plt.pcolormesh(xx, yy, ynew)
>>> plt.scatter(x[:,0], x[:,1], c=y)
>>> plt.show()

```



## 9.2 Kernel Adatron

**class** mlpy.**KernelAdatron** ( $C=1000$ ,  $maxsteps=1000$ ,  $eps=0.01$ )

Kernel Adatron algorithm without-bias-term (binary classifier).

The algorithm handles a version of the 1-norm soft margin support vector machine. If  $C$  is very high the algorithm handles a version of the hard margin SVM.



Use positive definite kernels (such as Gaussian and Polynomial kernels)

### Parameters

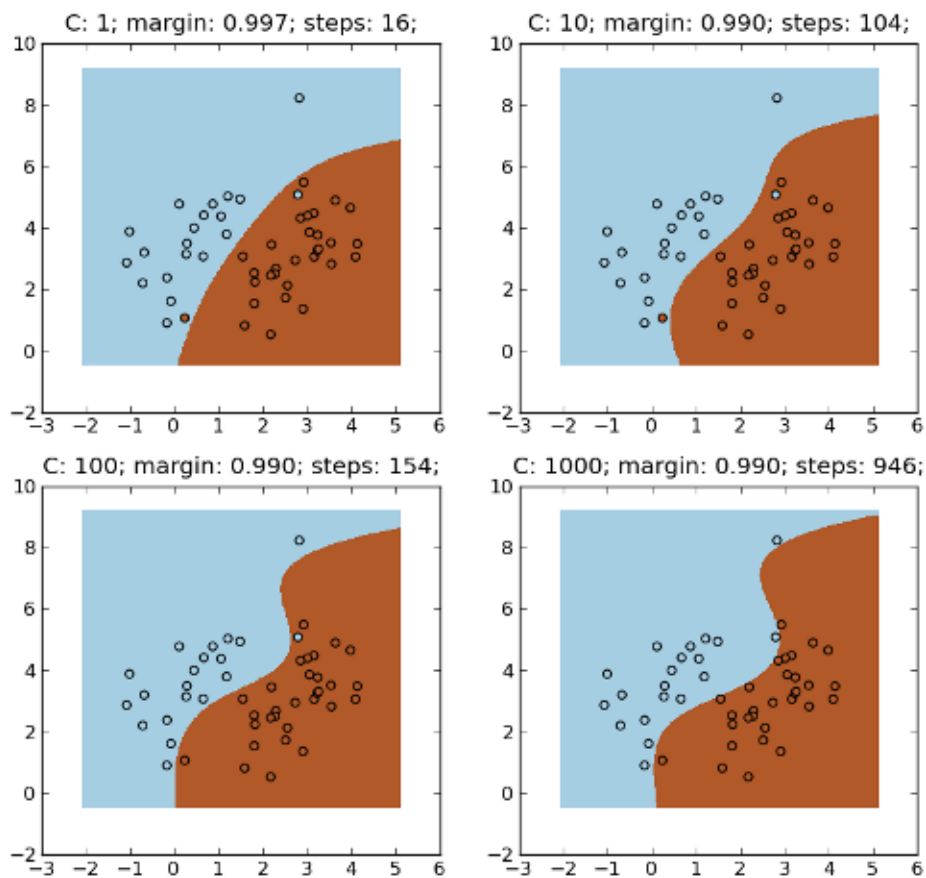
**C** [float] upper bound on the value of alpha

**maxsteps** [integer (> 0)] maximum number of steps

**eps** [float (>=0)] the algorithm stops when  $\text{abs}(1 - \text{margin}) < \text{eps}$

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 4.5], [[1,1],[1,2]], 20 # 20 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,1],[1,2]], 30 # 30 samples of class 2
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = 2 * np.ones(n2, dtype=np.int)
>>> x = np.concatenate((x1, x2), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2))
>>> K = mlpy.kernel_gaussian(x, x, sigma=2) # kernel matrix
>>> xmin, xmax = x[:,0].min()-1, x[:,0].max()+1
>>> ymin, ymax = x[:,1].min()-1, x[:,1].max()+1
>>> xx, yy = np.meshgrid(np.arange(xmin, xmax, 0.02), np.arange(ymin, ymax, 0.02))
>>> xt = np.c_[xx.ravel(), yy.ravel()] # test points
>>> Kt = mlpy.kernel_gaussian(xt, x, sigma=2) # test kernel matrix
>>> fig = plt.figure(1)
>>> cmap = plt.set_cmap(plt.cm.Paired)
>>> for i, c in enumerate([1, 10, 100, 1000]):
...     ka = mlpy.KernelAdatron(C=c)
...     ax = plt.subplot(2, 2, i+1)
...     ka.learn(K, y)
...     ytest = ka.pred(Kt).reshape(xx.shape)
...     title = ax.set_title('C: %s; margin: %.3f; steps: %s;' % (c, ka.margin(), ka.
->steps()))
...     plot1 = plt.pcolormesh(xx, yy, ytest)
...     plot2 = plt.scatter(x[:,0], x[:,1], c=y)
>>> plt.show()
```



## LARGE LINEAR CLASSIFICATION FROM [LIBLINEAR]

Solvers:

- **l2r\_lr**: L2-regularized logistic regression (primal)
- **l2r\_l2loss\_svc\_dual**: L2-regularized L2-loss support vector classification (dual)
- **l2r\_l2loss\_svc**: L2-regularized L2-loss support vector classification (primal)
- **l2r\_l1loss\_svc\_dual**: L2-regularized L1-loss support vector classification (dual)
- **mcsvm\_cs**: multi-class support vector classification by Crammer and Singer
- **l1r\_l2loss\_svc**: L1-regularized L2-loss support vector classification
- **l1r\_lr**: L1-regularized logistic regression
- **l2r\_lr\_dual**: L2-regularized logistic regression (dual)

**class** `mlpy.LibLinear` (*solver\_type='l2r\_lr', C=1, eps=0.01, weight={}*)

LibLinear is a simple class for solving large-scale regularized linear classification. It currently supports L2-regularized logistic regression/L2-loss support vector classification/L1-loss support vector classification, and L1-regularized L2-loss support vector classification/ logistic regression.

### Parameters

**solver\_type** [string] solver, can be one of 'l2r\_lr', 'l2r\_l2loss\_svc\_dual', 'l2r\_l2loss\_svc', 'l2r\_l1loss\_svc\_dual', 'mcsvm\_cs', 'l1r\_l2loss\_svc', 'l1r\_lr', 'l2r\_lr\_dual'

**C** [float] cost of constraints violation

**eps** [float] stopping criterion

**weight** [dict] changes the penalty for some classes (if the weight for a class is not changed, it is set to 1). For example, to change penalty for classes 1 and 2 to 0.5 and 0.8 respectively set `weight={1:0.5, 2:0.8}`

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 5], [[1,1],[1,2]], 200 # 200 samples of class 0
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.zeros(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,0],[0,1]], 300 # 300 samples of class 1
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = np.ones(n2, dtype=np.int)
>>> mean3, cov3, n3 = [5, 8], [[0.5,0],[0,0.5]], 200 # 200 samples of class 2
```

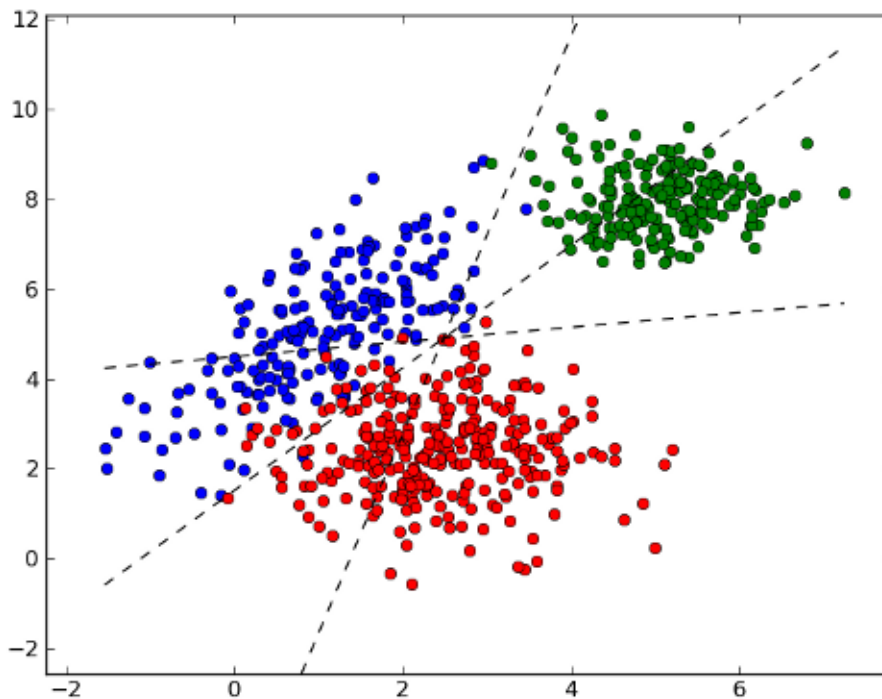
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```

>>> x3 = np.random.multivariate_normal(mean3, cov3, n3)
>>> y3 = 2 * np.ones(n3, dtype=np.int)
>>> x = np.concatenate((x1, x2, x3), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2, y3))
>>> svm = mlpy.LibLinear(solver_type='l2r_l2loss_svc_dual', C=0.01)
>>> svm.learn(x, y)
>>> w = svm.w() # w[i]: coefficients for label svm.labels()[i]
>>> w
array([[ -0.73225278,  0.33309388],
       [ 0.32295557, -0.44097029],
       [ 0.23192595,  0.11536679]])
>>> b = svm.bias() # b[i]: bias for label svm.labels()[i]
>>> b
array([ -0.21631629,  0.96014472, -1.53933202])
>>> xx = np.arange(np.min(x[:,0]), np.max(x[:,0]), 0.01)
>>> yy1 = (xx * (w[1][0]-w[0][0]) + b[1] - b[0]) / (w[0][1]-w[1][1])
>>> yy2 = (xx * (w[2][0]-w[0][0]) + b[2] - b[0]) / (w[0][1]-w[2][1])
>>> yy3 = (xx * (w[2][0]-w[1][0]) + b[2] - b[1]) / (w[1][1]-w[2][1])
>>> fig = plt.figure(1) # plot
>>> plot1 = plt.plot(x1[:, 0], x1[:, 1], 'ob', x2[:, 0], x2[:, 1], 'or', x3[:, 0],
↳ x3[:, 1], 'og')
>>> plot2 = plt.plot(xx, yy1, '--k')
>>> plot3 = plt.plot(xx, yy2, '--k')
>>> plot4 = plt.plot(xx, yy3, '--k')
>>> plt.show()

```



```

>>> test = [[6,7], [4, 2]] # test points

```

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```
>>> print svm.pred(test)
array([2, 1])
```



## CLUSTER ANALYSIS

### 11.1 Hierarchical Clustering

Hierarchical Clustering algorithm derived from the R package ‘[amap](#)’ [[Amap](#)].

The condensed distance matrix `y` can be computed by `pdist()` function in **scipy** (<<http://docs.scipy.org/doc/scipy/reference/spatial.distance.html>>)

### 11.2 Memory-saving Hierarchical Clustering

Memory-saving Hierarchical Clustering derived from the R and Python package ‘[fastcluster](#)’ [[fastcluster](#)].

### 11.3 k-means

`mlpy.kmeans(x, k, plus=False, seed=0)`

k-means clustering.

#### Parameters

**x** [2d array\_like object (N, P)] data

**k** [int (1<k<N)] number of clusters

**plus** [bool] k-means++ algorithm for initialization

**seed** [int] random seed for initialization

#### Returns

**clusters, means, steps:** 1d array, 2d array, int cluster membership in 0, ..., K-1, means (K,P), number of steps

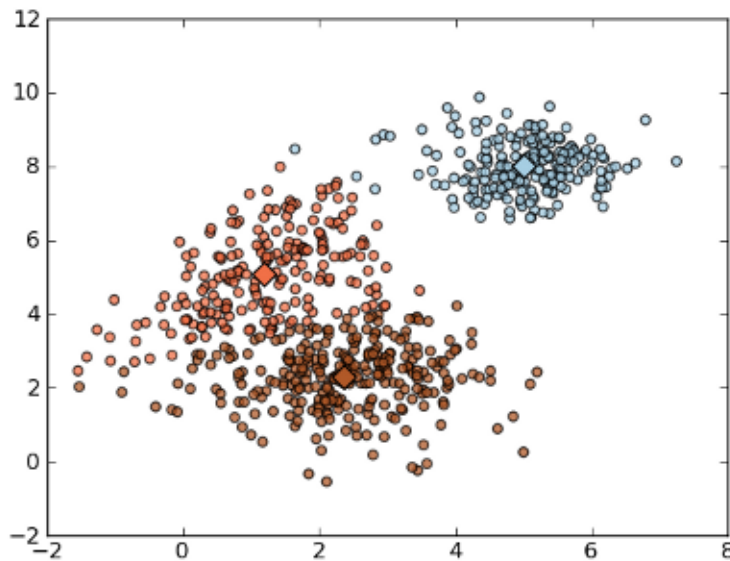
Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 5], [[1,1],[1,2]], 200 # 200 points, mean=(1,5)
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,0],[0,1]], 300 # 300 points, mean=(2.5,2.5)
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
```

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```
>>> mean3, cov3, n3 = [5, 8], [[0.5,0],[0,0.5]], 200 # 200 points, mean=(5,8)
>>> x3 = np.random.multivariate_normal(mean3, cov3, n3)
>>> x = np.concatenate((x1, x2, x3), axis=0) # concatenate the samples
>>> cls, means, steps = mlpy.kmeans(x, k=3, plus=True)
>>> steps
13
>>> fig = plt.figure(1)
>>> plot1 = plt.scatter(x[:,0], x[:,1], c=cls, alpha=0.75)
>>> plot2 = plt.scatter(means[:,0], means[:,1], c=np.unique(cls), s=128, marker='d')
↪ # plot the means
>>> plt.show()
```





## ALGORITHMS FOR FEATURE WEIGHTING

### 12.1 Iterative RELIEF



## FEATURE SELECTION

### 13.1 Recursive Feature Elimination



## DIMENSIONALITY REDUCTION

### 14.1 Linear Discriminant Analysis (LDA)

Example:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlp
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 4.5], [[1,1],[1,2]], 20 # 20 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,1],[1,2]], 30 # 30 samples of class 2
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = 2 * np.ones(n2, dtype=np.int)
>>> x = np.concatenate((x1, x2), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2))
>>> lda = mlp.LDA()
>>> lda.learn(x, y) # compute the tranformation matrix
>>> z = lda.transform(x) # embedded x into the C-1 = 1 dimensional space
```

### 14.2 Spectral Regression Discriminant Analysis (SRDA)

### 14.3 Kernel Fisher Discriminant Analysis (KFDA)

Example - KNN in kernel fisher space:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlp
>>> np.random.seed(0)
>>> mean1, cov1, n1 = [1, 4.5], [[1,1],[1,2]], 20 # 20 samples of class 1
>>> x1 = np.random.multivariate_normal(mean1, cov1, n1)
>>> y1 = np.ones(n1, dtype=np.int)
>>> mean2, cov2, n2 = [2.5, 2.5], [[1,1],[1,2]], 30 # 30 samples of class 2
>>> x2 = np.random.multivariate_normal(mean2, cov2, n2)
>>> y2 = 2 * np.ones(n2, dtype=np.int)
>>> x = np.concatenate((x1, x2), axis=0) # concatenate the samples
>>> y = np.concatenate((y1, y2))
>>> K = mlp.kernel_gaussian(x, x, sigma=3) # compute the kernel matrix
```

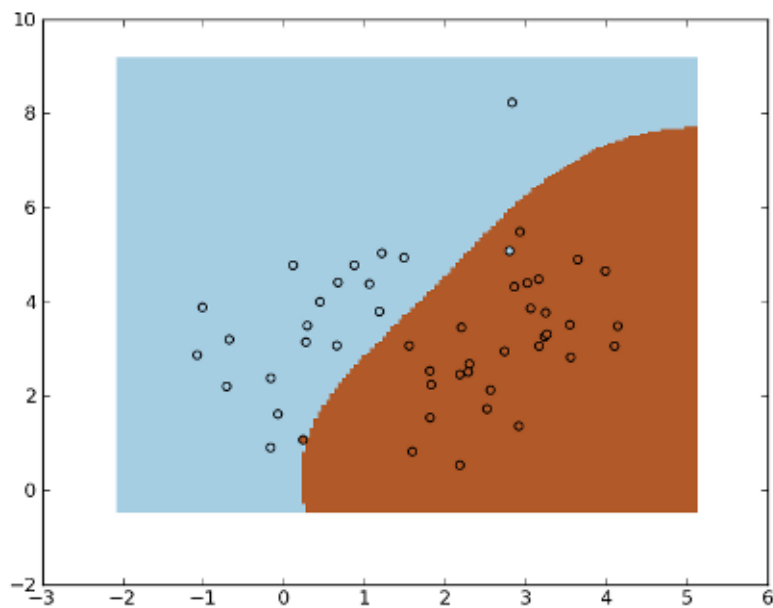
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```

>>> kfda = mlpy.KFDA(lmb=0.01)
>>> kfda.learn(K, y) # compute the tranformation vector
>>> z = kfda.transform(K) # embedded x into the kernel fisher space
>>> knn = mlpy.KNN(k=5)
>>> knn.learn(z, y) # learn KNN in the kernel fisher space
>>> xmin, xmax = x[:,0].min()-1, x[:,0].max()+1
>>> ymin, ymax = x[:,1].min()-1, x[:,1].max()+1
>>> xx, yy = np.meshgrid(np.arange(xmin, xmax, 0.05), np.arange(ymin, ymax, 0.05))
>>> xt = np.c_[xx.ravel(), yy.ravel()]
>>> Kt = mlpy.kernel_gaussian(xt, x, sigma=3) # compute the kernel matrix Kt
>>> zt = kfda.transform(Kt) # embedded xt into the kernel fisher space
>>> yt = KNN.pred(zt).reshape(xx.shape) # perform the KNN prediction in the kernel_
↳fisher space
>>> fig = plt.figure(1)
>>> cmap = plt.set_cmap(plt.cm.Paired)
>>> plot1 = plt.pcolormesh(xx, yy, yt)
>>> plot2 = plt.scatter(x[:,0], x[:,1], c=y)
>>> plt.show()

```



## 14.4 Principal Component Analysis (PCA)

Example:

```

>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> mean, cov, n = [0, 0], [[1,1],[1,1.5]], 100
>>> x = np.random.multivariate_normal(mean, cov, n)

```

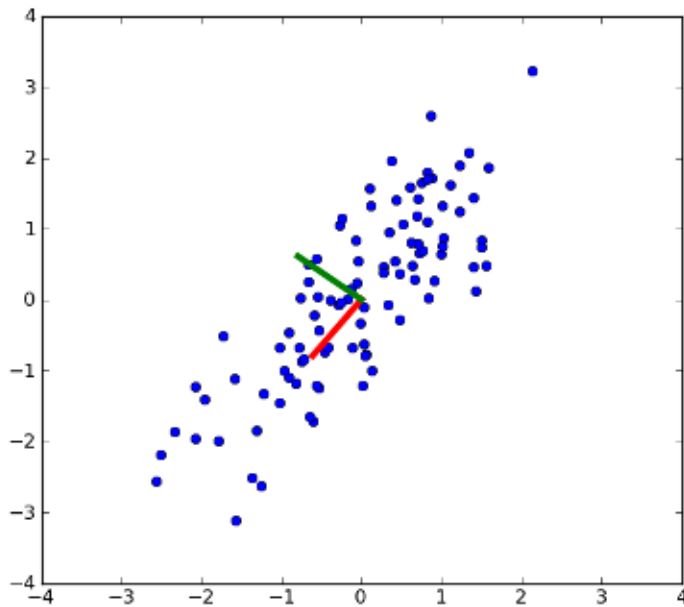
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```

>>> pca.learn(x)
>>> coeff = pca.coeff()
>>> fig = plt.figure(1) # plot
>>> plot1 = plt.plot(x[:, 0], x[:, 1], 'o')
>>> plot2 = plt.plot([0,coeff[0, 0]], [0, coeff[1, 0]], linewidth=4, color='r') #
↪first PC
>>> plot3 = plt.plot([0,coeff[0, 1]], [0, coeff[1, 1]], linewidth=4, color='g') #
↪second PC
>>> xx = plt.xlim(-4, 4)
>>> yy = plt.ylim(-4, 4)
>>> plt.show()

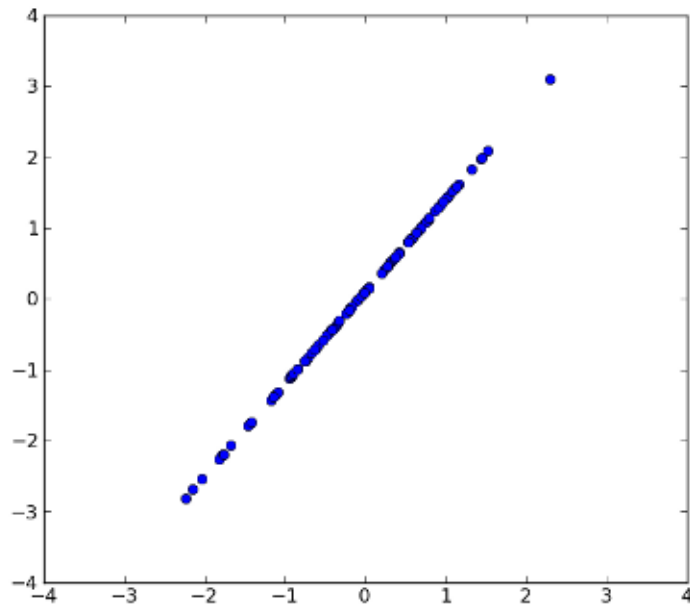
```



```

>>> z = pca.transform(x, k=1) # transform x using the first PC
>>> xnew = pca.transform_inv(z) # transform data back to its original space
>>> fig2 = plt.figure(2) # plot
>>> plot1 = plt.plot(xnew[:, 0], xnew[:, 1], 'o')
>>> xx = plt.xlim(-4, 4)
>>> yy = plt.ylim(-4, 4)
>>> plt.show()

```



## 14.5 Fast Principal Component Analysis (PCAFast)

Fast PCA implementation described in [Sharma07].

Example reproducing Figure 1 of [Sharma07]:

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> h = 10 # dimension reduced to h=10
>>> n = 100 # number of samples
>>> d = np.array([100, 200, 300, 400, 500, 600, 700, 800, 900, 1000, 2000, 3000,
↳4000]) # number of dimensions
>>> mse_eig, mse_fast = np.zeros(len(d)), np.zeros(len(d))
>>> pca = mlpy.PCA(method='cov') # pca (eigenvalue decomposition)
>>> pca_fast = mlpy.PCAFast(k=h) # fast pca
>>> for i in range(d.shape[0]):
...     x = np.random.rand(n, d[i])
...     pca.learn(x) # pca (eigenvalue decomposition)
...     y_eig = pca.transform(x, k=h) # reduced dimensional feature vectors
...     xhat_eig = pca.transform_inv(y_eig) # reconstructed vector
...     pca_fast.learn(x) # pca (eigenvalue decomposition)
...     y_fast = pca_fast.transform(x) # reduced dimensional feature vectors
...     xhat_fast = pca_fast.transform_inv(y_fast) # reconstructed vector
...     for j in range(n):
...         mse_eig[i] += np.sum((x[j] - xhat_eig[j])**2)
...         mse_fast[i] += np.sum((x[j] - xhat_fast[j])**2)
...     mse_eig[i] /= n
...     mse_fast[i] /= n
... 
```

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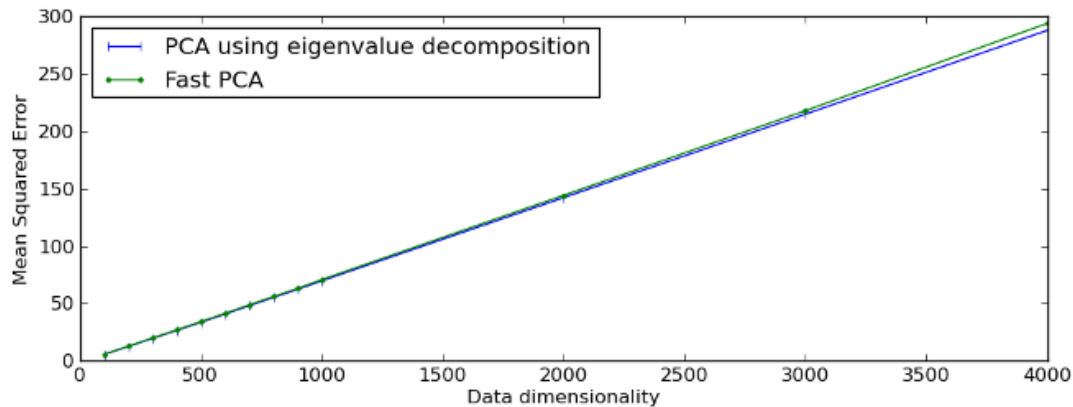


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```

>>> fig = plt.figure(1)
>>> plot1 = plt.plot(d, mse_eig, '|-b', label="PCA using eigenvalue decomposition")
>>> plot2 = plt.plot(d, mse_fast, '-g', label="Fast PCA")
>>> leg = plt.legend(loc = 'best')
>>> xl = plt.xlabel("Data dimensionality")
>>> yl = plt.ylabel("Mean Squared Error")
>>> plt.show()

```



## 14.6 Kernel Principal Component Analysis (KPCA)

Example:

```

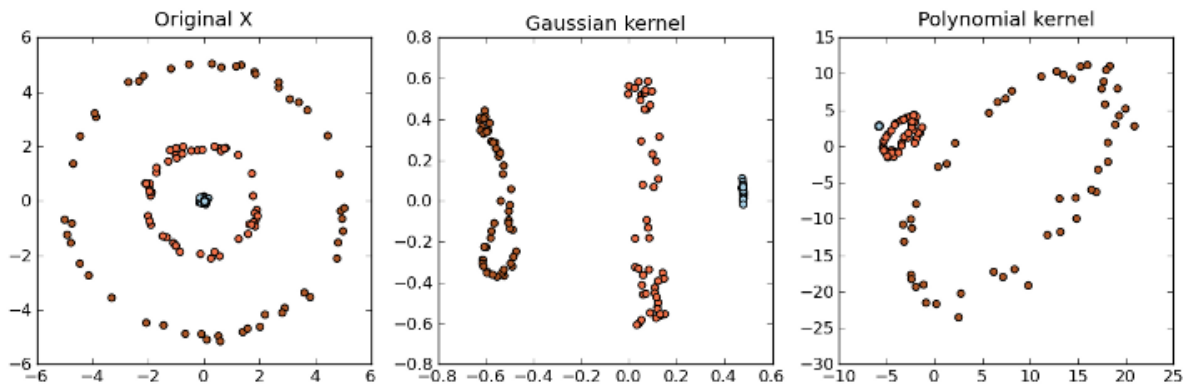
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlpy
>>> np.random.seed(0)
>>> np.random.seed(0)
>>> x = np.zeros((150, 2))
>>> y = np.empty(150, dtype=np.int)
>>> theta = np.random.normal(0, np.pi, 50)
>>> r = np.random.normal(0, 0.1, 50)
>>> x[0:50, 0] = r * np.cos(theta)
>>> x[0:50, 1] = r * np.sin(theta)
>>> y[0:50] = 0
>>> theta = np.random.normal(0, np.pi, 50)
>>> r = np.random.normal(2, 0.1, 50)
>>> x[50:100, 0] = r * np.cos(theta)
>>> x[50:100, 1] = r * np.sin(theta)
>>> y[50:100] = 1
>>> theta = np.random.normal(0, np.pi, 50)
>>> r = np.random.normal(5, 0.1, 50)
>>> x[100:150, 0] = r * np.cos(theta)
>>> x[100:150, 1] = r * np.sin(theta)
>>> y[100:150] = 2
>>> cmap = plt.set_cmap(plt.cm.Paired)
>>> gK = mlpy.kernel_gaussian(x, x, sigma=2) # gaussian kernel matrix
>>> pK = mlpy.kernel_polynomial(x, x, gamma=1.0, b=1.0, d=2.0) # polynomial kernel_
↪matrix

```

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```
>>> gaussian_pca = mlpy.KPCA()
>>> polynomial_pca = mlpy.KPCA()
>>> gaussian_pca.learn(gK)
>>> polynomial_pca.learn(pK)
>>> gz = gaussian_pca.transform(gK, k=2)
>>> pz = polynomial_pca.transform(pK, k=2)
>>> fig = plt.figure(1)
>>> ax1 = plt.subplot(131)
>>> plot1 = plt.scatter(x[:, 0], x[:, 1], c=y)
>>> title1 = ax1.set_title('Original X')
>>> ax2 = plt.subplot(132)
>>> plot2 = plt.scatter(gz[:, 0], gz[:, 1], c=y)
>>> title2 = ax2.set_title('Gaussian kernel')
>>> ax3 = plt.subplot(133)
>>> plot3 = plt.scatter(pz[:, 0], pz[:, 1], c=y)
>>> title3 = ax3.set_title('Polynomial kernel')
>>> plt.show()
```



## CROSS VALIDATION

### 15.1 Leave-one-out and k-fold

### 15.2 Random Subsampling (*aka MonteCarlo*)

### 15.3 All Combinations



## METRICS

Compute metrics for assessing the performance of classification/regression models.

### 16.1 Classification

Examples:

```
>>> import mlp
>>> t = [3,2,3,3,3,1,1,1]
>>> p = [3,2,1,3,3,2,1,1]
>>> mlp.error(t, p)
0.25
>>> mlp.accuracy(t, p)
0.75
```

#### 16.1.1 Binary Classification Only

The Confusion Matrix:

Total Samples (ts)	Actual Positives (ap)	Actual Negatives (an)
Predicted Positives (pp)	True Positives (tp)	False Positives (fp)
Predicted Negatives (pn)	False Negatives (fn)	True Negatives (tn)

Examples:

```
>>> import mlp
>>> t = [1, 1, 1,-1, 1,-1,-1,-1]
>>> p = [1,-1, 1, 1, 1,-1, 1,-1]
>>> mlp.error_p(t, p)
0.25
>>> mlp.error_n(t, p)
0.5
>>> mlp.sensitivity(t, p)
0.75
>>> mlp.specificity(t, p)
0.5
>>> mlp.ppv(t, p)
0.5999999999999998
>>> mlp.npv(t, p)
0.6666666666666663
```

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```
>>> mlp.py.mcc(t, p)
0.2581988897471611
>>> p = [2.3, -0.4, 1.6, 0.6, 3.2, -4.9, 1.3, -0.3]
>>> mlp.py.auc_wmw(t, p)
0.8125
>>> p = [2.3, 0.4, 1.6, -0.6, 3.2, -4.9, -1.3, -0.3]
>>> mlp.py.auc_wmw(t, p)
1.0
```

## 16.2 Regression

Example:

```
>>> import mlp.py
>>> t = [2.4, 0.4, 1.2, -0.2, 3.3, -4.9, -1.1, -0.1]
>>> p = [2.3, 0.4, 1.6, -0.6, 3.2, -4.9, -1.3, -0.3]
>>> mlp.py.mse(t, p)
0.052499999999999998
```

**A SET OF STATISTICAL FUNCTIONS**





## CANBERRA DISTANCES AND STABILITY INDICATOR OF RANKED LISTS

### 18.1 Canberra distance

### 18.2 Canberra Distance with Location Parameter

See [Jurman08].

The function computes:

$$\sum_i \frac{|\min\{x_i + 1, k + 1\} - \min\{y_i + 1, k + 1\}|}{\min\{x_i + 1, k + 1\} + \min\{y_i + 1, k + 1\}}$$

### 18.3 Canberra Stability Indicator

See [Jurman08].



**BORDA COUNT**



---

CHAPTER  
**TWENTY**

---

**FIND PEAKS**



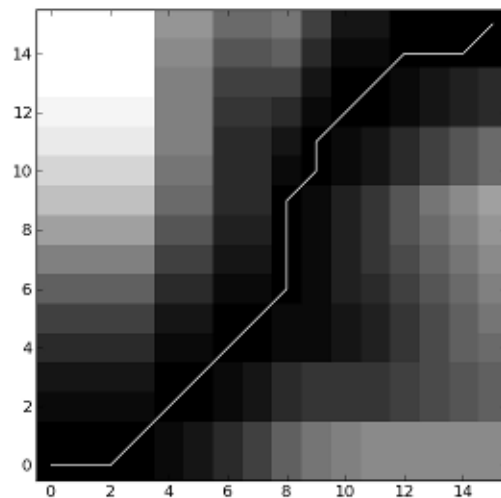
## DYNAMIC TIME WARPING (DTW)

### 21.1 Standard DTW

Example

Reproducing the Fig. 2 example in [Salvador04].

```
>>> import mlp
>>> import matplotlib.pyplot as plt
>>> import matplotlib.cm as cm
>>> x = [0,0,0,0,1,1,2,2,3,2,1,1,0,0,0,0]
>>> y = [0,0,1,1,2,2,3,3,3,3,2,2,1,1,0,0]
>>> dist, cost, path = mlp.dtw_std(x, y, dist_only=False)
>>> dist
0.0
>>> fig = plt.figure(1)
>>> ax = fig.add_subplot(111)
>>> plot1 = plt.imshow(cost.T, origin='lower', cmap=cm.gray, interpolation='nearest')
>>> plot2 = plt.plot(path[0], path[1], 'w')
>>> xlim = ax.set_xlim((-0.5, cost.shape[0]-0.5))
>>> ylim = ax.set_ylim((-0.5, cost.shape[1]-0.5))
>>> plt.show()
```



## 21.2 Subsequence DTW



## LONGEST COMMON SUBSEQUENCE (LCS)

### 22.1 Standard LCS

### 22.2 LCS for real series



## MLPY . WAVELET - WAVELET TRANSFORM

### 23.1 Padding

### 23.2 Discrete Wavelet Transform

Discrete Wavelet Transform based on the GSL DWT [GslDwt].

For the forward transform, the output is the discrete wavelet transform  $f_i \rightarrow w_{j,k}$  in a packed triangular storage layout, where  $j$  is the index of the level  $j = 0 \dots J-1$  and  $k$  is the index of the coefficient within each level,  $k = 0 \dots (2^j) - 1$ . The total number of levels is  $J = \log_2(n)$ . The output data has the following form,

$$(s_{-1,0}, d_{0,0}, d_{1,0}, d_{1,1}, d_{2,0}, \dots, d_{j,k}, \dots, d_{J-1,2^{J-1}-1})$$

where the first element is the smoothing coefficient  $s_{-1,0}$ , followed by the detail coefficients  $d_{j,k}$  for each level  $j$ . The backward transform inverts these coefficients to obtain the original data.

---

**Note:** from GSL online manual (<http://www.gnu.org/software/gsl/manual/>)

---

### 23.3 Undecimated Wavelet Transform

Undecimated Wavelet Transform (also known as stationary wavelet transform, redundant wavelet transform, translation invariant wavelet transform, shift invariant wavelet transform or Maximal overlap wavelet transform) based on the “wavelets” R package.

### 23.4 Continuous Wavelet Transform

Continuous Wavelet Transform based on [Torrence98].

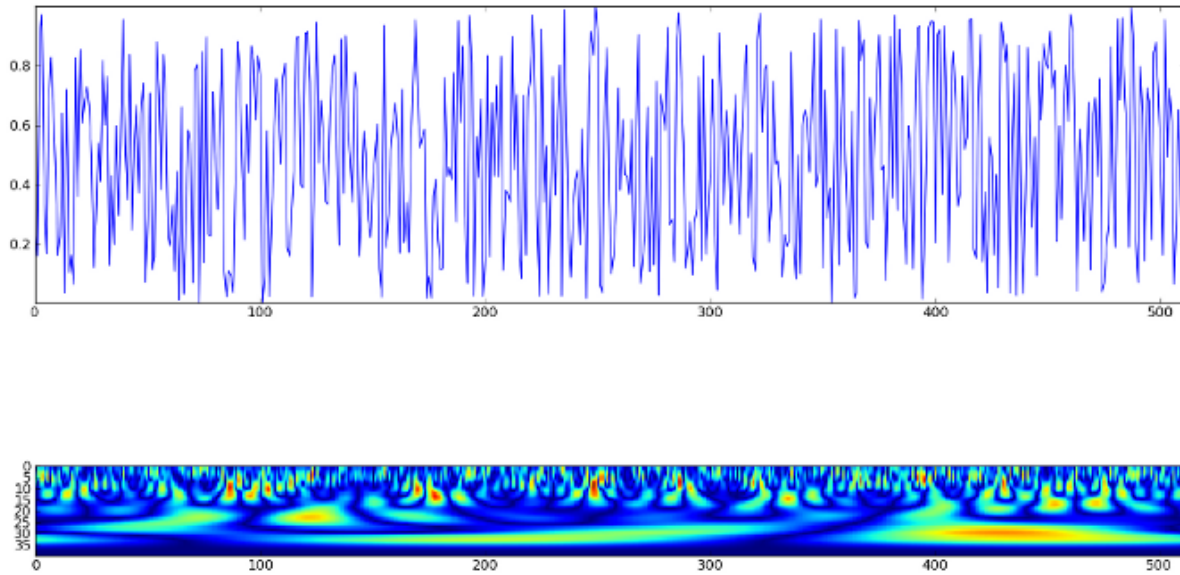
Example (requires matplotlib)

```
>>> import numpy as np
>>> import matplotlib.pyplot as plt
>>> import mlp.wavelet as wave
>>> x = np.random.sample(512)
>>> scales = wave.autoscales(N=x.shape[0], dt=1, dj=0.25, wf='dog', p=2)
>>> X = wave.cwt(x=x, dt=1, scales=scales, wf='dog', p=2)
>>> fig = plt.figure(1)
```

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```
>>> ax1 = plt.subplot(2,1,1)
>>> p1 = ax1.plot(x)
>>> ax1.autoscale_view(tight=True)
>>> ax2 = plt.subplot(2,1,2)
>>> p2 = ax2.imshow(np.abs(X), interpolation='nearest')
>>> plt.show()
```



## SHORT GUIDE TO CENTERING AND SCALING

Centering:

1d array	<pre>&gt;&gt;&gt; x - np.mean(x)</pre>
2d array along rows	<pre>&gt;&gt;&gt; x - np.mean(x, axis=1).reshape(-1, 1)</pre>
2d array along cols	<pre>&gt;&gt;&gt; x - np.mean(x, axis=0)</pre>

Unit length scaling (normalization). Elements are scaled to have and unit length ( $\sum_{i=1}^n x_i^2 = 1$ ):

1d array	<pre>&gt;&gt;&gt; x / np.sqrt(np.sum((x)**2))</pre>
2d array along rows	<pre>&gt;&gt;&gt; x / np.sqrt(np.sum((x)**2, axis=1)). ↳ reshape(-1, 1)</pre>
2d array along cols	<pre>&gt;&gt;&gt; x / np.sqrt(np.sum((x)**2, axis=0))</pre>

Standardization. Elements are scaled to have unit standard deviation. The standard deviation is computed using  $n - 1$  instead of  $n$  (Bessel's correction).

1d array	<pre>&gt;&gt;&gt; x / np.std(x, ddof=1) # ddof=1:  ↳ Bessel's correction</pre>
2d array along rows	<pre>&gt;&gt;&gt; x / np.std(x, axis=1, ddof=1). ↳ reshape(-1, 1)</pre>
2d array along cols	<pre>&gt;&gt;&gt; x / np.std(x, axis=0, ddof=1)</pre>



## INDICES AND TABLES

- `genindex`
- `modindex`
- `search`





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